TED (15) - 1002	Reg. No.
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# FIRST SEMESTER DIPLOMA EXAMINATION IN ENGINEERING/TECHNOLOGY — APRIL, 2017

## ENGINEERING MATHEMATICS - I

(Common to all Diploma Programmes)

[Time: 3 hours

(Maximum marks: 100)

PART --- A

(Maximum marks: 10)

Marks

- I Answer all questions. Each question carries 2 marks.
  - 1. Evaluate Lt  $\frac{x^3 27}{x 3}$
  - 2. If  $\tan A = 3/4$  and A is acute, find  $\sin 2A$ .
  - 3. In a triangle ABC,  $A = 45^{\circ}$   $B = 60^{\circ}$  a = 5cm. Find b.
  - 4. Evaluate  $4 \sin^3 60 3\cos 30$ .
  - 5. Find the slope of the curve  $y = 3x^2 + x 2$  at (1, 2).  $(5 \times 2 = 10)$

#### PART---B

(Maximum marks: 30)

- II Answer any five questions from the following. Each question carries 6 marks.
  - 1. Express  $\sqrt{3}\cos x + \sin x$  in the form R  $\sin (x + \alpha)$  where  $\alpha$  is acute.
  - 2. If  $A + B = 45^{\circ}$ , show that  $(1 + \tan A) (1 + \tan B) = 2$ .
  - 3. Show that  $\cos 20^\circ \cos 40^\circ \cos 60^\circ \cos 80^\circ = \frac{1}{16}$ .
  - 4. Differentiate 'sin x' by method of first principles.
  - 5. If  $y = x^2 \sin x$  prove that  $x^2y'' 4xy' + (x^2 + 6) y = 0$ .
  - 6. The distance S metres travelled by a particle is given by  $S = ae^{nt} + be^{-nt}$  where t represents the time. Show that the acceleration varies as the distance.
  - 7. A balloon is spherical in shape. Gas is escaping from it at the rate of 10cc/sec. How fast is the surface area shrinking, when the radius is 15cm.

 $(5 \times 6 - 30)$ 

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#### PART - C

## (Maximum marks: 60)

(Answer one full question from each unit. Each full question carries 15 marks.)

## Unit -- I

- III (a) Prove that  $\frac{cosec \ \theta}{cosec \ \theta 1} + \frac{cosec \ \theta}{cosec \ \theta + 1} = 2 \ sec^2 \theta$ 
  - (b) If tan A = 3/4, sin B = 5/13. A lies in third quadrant and B lies in second quadrant. Find sin(A B) and cos(A + B).
  - (c) Evaluate cos570 sin510 sin330 cos390.

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- IV (a) Prove that  $\sin(\pi/3 + A) \sin(\pi/3 A) = \sin A$ .
  - (b) If tanx = 7/24 and x is in 3rd quadrant. Find the value of 3 sinx 4 cosx.
  - (c) Find the value of  $\tan 75$  without using tables and show that  $\tan 75 + \cot 75 = 4$ .

# Unit -- II

- $\dot{V}$  (a) Prove that  $\frac{(\sin 2A + \sin 5A \sin A)}{\cos 2A + \cos 5A + \cos A} = \tan 2A$ .
  - (b) Show that  $\frac{1 + \cos 2A}{\sin 2A} = \cot A$  and deduce the value of cot 15.
  - (c) Solve triangle ABC, given a = 4cm b = 5cm c = 7cm.

#### Or

- VI (a) Prove that  $\frac{\sin 3A}{\sin A} \frac{\cos 3A}{\cos A} = 2$ .
  - (b) Show that  $\cos 55 + \cos 65 + \cos 175 = 0$ .
  - (c) Prove that  $R(a^2 + b^2 + c^2) = abc(cotA + cotB + cotC)$ .

#### UNIT - III

- VII (a) Evaluate: Lt  $\frac{x^3-64}{x^2-16}$ 
  - (b) Find  $\frac{dy}{dx}$ , if (i)  $y = \log \sin \sqrt{x}$  (ii)  $\frac{(x^2 \sec x)}{(x^2 + 3)}$
  - (c) If x = a (cost + t sint) y = a(sint tcost), find  $\frac{dy}{dx}$

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- VIII (a) Find  $\frac{dy}{dx}$  if: (i)  $y = \cot^5(x^2)$  (ii)  $\frac{\sin(\log x)}{x}$ 
  - (b) Find  $\frac{dy}{dx}$ , if  $x^2y^2 = x^3 + y^3 + 3xy$ .
  - (c) Find the derivative of cotx using quotient rule.

### Unit -- IV

5 IX (a) Find the equations to the tangent and normal to the curve  $y = \cos x$  at  $x = \pi/6$ . (b) If S denotes the displacement of a-particle at the time t sees and  $S = t^3 - 6t^2 + 8t - 4$ , find the time when the acceleration is 12cm/sec<sup>2</sup>. Find the velocity at that time. 5 (c) The deflection of a beam is given by  $y = 2x^3 - 9x^2 + 12x$ . Find the maximum 5 deflection.  $O_R$ X (a) Find the values of x for which the tangent to the curve  $y = \frac{x}{(1-x)^2}$  will be parallel to the (i) X axis, (ii) Y axis 5 (b) A spherical rubber bladder of radius 3" has air pumped into it. If the radius increases at a uniform rate of 1" per minute, find the rate at which the volume is increasing at the end of 3 minutes. 5 (c) The sum of the diameter and length of an open cylindrical vessel is 40cm. Prove that the maximum volume is obtained. When the radius is equal to 5 the length?